

Probing anomalous **VZH** couplings at ILC with polarized beams

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Work is done in collaboration with : Prof. Saurabh D. Rindani

- ▶ Phys. Lett. B **693** (2010), arXiv:1001.4931[hep-ph]
- ▶ Phys. Rev. D **79** (2009), arXiv:0901.2821[hep-ph]

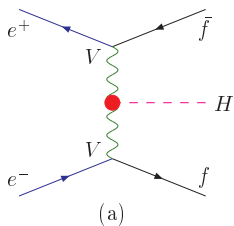
December 16, 2010

- ▶ EWSB predicts a fundamental scalar known as the Higgs
- ▶ In SM, there is one CP even neutral Higgs
- ▶ The aim of current (LHC) and future (ILC, CLIC) colliders is to discover the Higgs
- ▶ Some models like MSSM, 2HDM etc. predict existence of more than one Higgs
- ▶ Even if one discovers a Higgs, it is not a confirmation for SM Higgs

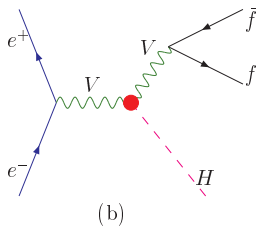
- ▶ For this, a thorough study is needed to study its properties
- ▶ Which is easier at e^+e^- linear colliders than hadron colliders.
- ▶ Any deviation in SM values of the Higgs couplings would be a signal of new physics
- ▶ Higgs couplings are proportional to mass of particle which it couples,
- ▶ Interesting to study Higgs interactions with heavier particles like top quark and the electroweak bosons

Higgs @ ILC

$$\begin{array}{lcl}
 e^+e^- & \rightarrow & e^+e^-Z^*Z^* \rightarrow e^+e^-H \quad (\text{Z-fusion}) \\
 & \rightarrow & \nu_e\bar{\nu}_eW^*W^* \rightarrow \nu_e\bar{\nu}_eH \quad (\text{W-fusion}) \\
 & \rightarrow & ZH \rightarrow f\bar{f}H \quad (\text{Bjorken})
 \end{array}$$



(a) Gauge Boson Fusion



(b) Bjorken

The process $e^+e^- \rightarrow \nu_e\bar{\nu}_eH$ has the **highest rate** for an intermediate mass Higgs boson.

- ▶ Full potential of ILC can only be utilized with polarization of beams,
- ▶ Earlier, **SLAC** used polarized e^- beams for **SLD** experiment,
- ▶ **80%** of e^- polarization has been achieved at **SLAC**,
- ▶ For **ILC**, **90%** e^- polarization is expected,
- ▶ For e^+ beam, **30%** polarization already achieved,
- ▶ For **ILC** expectation is **60%** polarization for e^+ beam,
- ▶ Both e^- and e^+ beam polarizations are important for studying new physics (will be discussed later),

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With unpolarized beams, cross section for e^+e^- annihilation process can be written as :

$$\sigma = \sigma_{LL} + \sigma_{RR} + \sigma_{RL} + \sigma_{LR}$$

With longitudinal polarization, cross section for e^+e^- annihilation process can be written as :

$$\begin{aligned}\sigma &= \frac{1 + P_L}{2} \frac{1 - \bar{P}_L}{2} \sigma_{\text{RL}} + \frac{1 - P_L}{2} \frac{1 + \bar{P}_L}{2} \sigma_{\text{LR}} \\ &= (1 - P_L \bar{P}_L) \left[\sigma_0 + \frac{P_L - \bar{P}_L}{1 - P_L \bar{P}_L} \frac{\sigma_{\text{RL}} - \sigma_{\text{LR}}}{4} \right] \\ &= (1 - P_L \bar{P}_L) \left[\sigma_0 + P_L^{\text{eff}} \frac{\sigma_{\text{RL}} - \sigma_{\text{LR}}}{4} \right]\end{aligned}$$

where $P_L^{\text{eff}} = \frac{P_L - \bar{P}_L}{1 - P_L \bar{P}_L}$ is “effective polarization”.

		P_L^{eff}	$\mathcal{L}_{\text{eff}}/\mathcal{L}$
$P_L = 0,$	$\bar{P}_L = 0$	0%	0.50
$P_L = 80\%,$	$\bar{P}_L = 0$	80%	0.50
$P_L = -80\%,$	$\bar{P}_L = 60\%$	-95%	0.74
$P_L = 80\%,$	$\bar{P}_L = 60\%$	39%	0.26

Role of longitudinal polarization

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- ▶ Increases signal,

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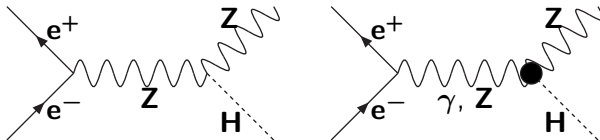
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- ▶ No need for measurement of polarizations of final state particles,
- ▶ probes couplings which are not accessible otherwise.

The process $e^+e^- \rightarrow HZ$

- ▶ We consider production of a Higgs through the process $e^+e^- \rightarrow HZ$ mediated by s-channel virtual γ and Z
- ▶ In SM, only contribution from s-channel exchange of Z at tree level
- ▶ No γZH couplings at tree level in SM, γ -exchange only at the loop level
- ▶ At the lowest order, the ZZH vertex in this diagram would be simply a point-like coupling



- ▶ Demanding Lorentz invariance, the general structure of the vertex $\mathbf{V}_\mu^*(\mathbf{k}_1) \rightarrow \mathbf{Z}_\nu^*(\mathbf{k}_2)\mathbf{H}$, where ($\mathbf{V} = \mathbf{Z}, \gamma$), can be expressed as (Hagiwara & Stong)¹

$$\Gamma_{\mu\nu} = g_V \left[a_V g_{\mu\nu} + \frac{b_V}{M_Z^2} (k_{1\nu} k_{2\mu} - g_{\mu\nu} \mathbf{k}_1 \cdot \mathbf{k}_2) + \frac{\tilde{b}_V}{M_Z^2} \epsilon_{\mu\nu\alpha\beta} k_1^\alpha k_2^\beta \right],$$

- ▶ a_V and b_V are **CP** - even, and \tilde{b}_V is **CP** - odd,
- ▶ We have studied these anomalous **VZH** ($\mathbf{V} = \gamma, \mathbf{Z}$) couplings at a linear collider in process $e^+e^- \rightarrow \mathbf{ZH}$,
- ▶ Couplings are taken to be complex, so six parameters to be determined in each case,

¹Z.Phys.C62 : 99 – 108, 1994

Recent works on **VVH** couplings at linear collider are of [Biswal](#)² et al., [Hagiwara](#)³ et al. and [Han](#)⁴ et al.

- ▶ [Biswal et al.](#) studied **ZZH** and **WWH** couplings at linear collider with polarized beams,
- ▶ They did not include γ **ZH** couplings in their analysis,
- ▶ [Hagiwara et al.](#) did include γ **ZH** couplings in their analysis,
- ▶ But, they use complicated techniques of b-tagging and measurement of final state τ polarization,
- ▶ [Han et al.](#) only considered **CP** odd **ZZH** couplings in their analysis

²Phys.Rev.D79 : 035012, Phys.Lett.B680 : 81 – 87

³Eur.Phys.J.C14 : 457 – 468, 2000

⁴Phys.Rev.D63 : 096007, 2001

- ▶ Obtain **analytical expressions** for angular distributions using both longitudinally and transversely polarized beams,
- ▶ Construct rather simpler observables like **asymmetry** and **correlations**,
- ▶ Observables are **simple** conceptually as well as experiment point of view,
- ▶ Observables have definite **CP** and **T** transformation properties,
- ▶ We make use of a combination of observables and/or polarizations,
- ▶ *Main emphasis on simultaneous independent determination of couplings,*

Unpolarized beams

$$\frac{d\sigma_{Z,\gamma}}{d\Omega} \propto \left[A^{Z,\gamma}(1 + \sin^2 \theta) + B^{Z,\gamma} + C^{Z,\gamma} \cos \theta \right]$$

	Z	γ	Couplings
A	$(g_V^2 + g_A^2)$	g_V	$\text{Re}\Delta_{az}, \text{Re}a_\gamma$
B	$(g_V^2 + g_A^2)$	g_V	$\text{Re}b_Z, \text{Re}b_\gamma$
C	$-2g_V g_A$	g_A	$\text{Im}\tilde{b}_Z, \text{Im}\tilde{b}_\gamma$

- ▶ $\text{Im}\Delta_{az}, \text{Im}a_\gamma, \text{Im}b_Z, \text{Im}b_\gamma, \text{Re}\tilde{b}_Z, \text{Re}\tilde{b}_\gamma$ are absent,
- ▶ $g_V = -0.12, g_A = -1,$

Longitudinally Polarized beams

$$\frac{d\sigma_{Z,\gamma}}{d\Omega} \propto (1 - P_L \bar{P}_L) \left[A^{Z,\gamma} (1 + \sin^2 \theta) + B^{Z,\gamma} + C^{Z,\gamma} \cos \theta \right]$$

	Z	γ	Couplings
A	$(g_V^2 + g_A^2) - 2g_V g_A P_L^{\text{eff}}$	$g_V - g_A P_L^{\text{eff}}$	$\text{Re}\Delta_{az}, \text{Re}a_\gamma$
B	$(g_V^2 + g_A^2) - 2g_V g_A P_L^{\text{eff}}$	$g_V - g_A P_L^{\text{eff}}$	$\text{Re}b_Z, \text{Re}b_\gamma$
C	$(g_V^2 + g_A^2) P_L^{\text{eff}} - 2g_V g_A$	$g_A - g_V P_L^{\text{eff}}$	$\text{Im}\tilde{b}_Z, \text{Im}\tilde{b}_\gamma$

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B	$(g_V^2 + g_A^2) - 2g_V g_A P_L^{\text{eff}}$	$g_V - g_A P_L^{\text{eff}}$	$\text{Re}b_Z, \text{Re}b_\gamma$
C	$(g_V^2 + g_A^2) P_L^{\text{eff}} - 2g_V g_A$	$g_A - g_V P_L^{\text{eff}}$	$\text{Im}\tilde{b}_Z, \text{Im}\tilde{b}_\gamma$

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- ▶ $g_V = -0.12, g_A = -1,$
- ▶ Non-trivial dependence on P_L^{eff}
- ▶ With P_L^{eff} , sensitivities to $\text{Re}a_\gamma, \text{Re}b_\gamma$ and $\text{Im}\tilde{b}_Z$ become significant.

- ▶ The terms proportional to $\cos \theta$ i.e., $\text{Im}\tilde{b}_Z, \text{Im}\tilde{b}_\gamma$ can be determined using a simple forward-backward asymmetry:

$$A_{FB}^L = \frac{\sigma(\cos \theta \geq 0) - \sigma(\cos \theta \leq 0)}{\sigma(\cos \theta \geq 0) + \sigma(\cos \theta \leq 0)},$$

$$\propto [\begin{matrix} & -2g_V g_A \\ g_A & \end{matrix}] \text{Im}\tilde{b}_Z$$

$$+ [g_A \quad \quad] \text{Im}\tilde{b}_\gamma$$

- ▶ 95% CL individual limits on $\text{Im}\tilde{b}_\gamma, \text{Im}\tilde{b}_Z$ using A_{FB}^L

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Unpolarized	0.00392	0.0108

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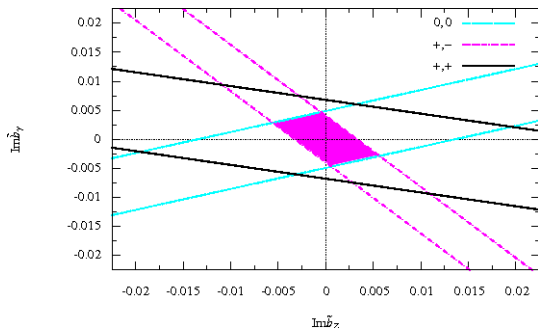
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- ▶ Sensitivity to $\text{Im}\tilde{b}_Z$ is enhanced by about a factor of 5 using opposite beam polarization because of the P_L^{eff}

As an illustration, we show a plot how we determine simultaneous limits using \mathbf{A}_{FB}



- ▶ (S.L.) are extremities of enclosed region.

The best simultaneous limits are region enclosed by the lines corresponding to $\mathbf{P}_L = \bar{\mathbf{P}}_L = \mathbf{0}$ and $(\mathbf{P}_L, \bar{\mathbf{P}}_L) = (0.8, -0.6)$:

$$|\text{Im}\tilde{b}_\gamma| \leq 4.69 \cdot 10^{-3}; |\text{Im}\tilde{b}_z| \leq 5.61 \cdot 10^{-3}.$$

With Transversely polarized beams

$$\frac{d\sigma_{Z,\gamma}^T}{d\Omega} \propto \left[\frac{d\sigma^{\text{SM}}}{d\Omega} + \mathbf{P}_T \bar{\mathbf{P}}_T \sin^2 \theta \left\{ \mathbf{D}_T^{Z,\gamma} \cos 2\phi + \mathbf{E}_T^\gamma \sin 2\phi \right\} \right]$$

- ▶ \mathbf{D}_T contains $\text{Re}\Delta\mathbf{a}_Z$ and $\text{Re}\mathbf{a}_\gamma$ while \mathbf{E}_T contains only $\text{Im}\mathbf{a}_\gamma$,
- ▶ Usefulness of TP comes from nontrivial ϕ dependence,
- ▶ Both electron and positron beams have to be polarized,
- ▶ $\text{Im}\mathbf{a}_\gamma$ is now accessible,
- ▶ *Most important result* : Independent determination of $\text{Im}\mathbf{a}_\gamma$ from the $\sin 2\phi$ term,
- ▶ $\text{Re}\tilde{\mathbf{b}}_Z$, $\text{Re}\tilde{\mathbf{b}}_\gamma$, $\text{Im}\mathbf{b}_Z$, $\text{Im}\mathbf{b}_\gamma$ and $\text{Im}\Delta\mathbf{a}_Z$ remain undetermined

- ▶ \mathbf{A}_T separate out coefficient of $\sin 2\phi$ i.e., $\text{Im} a_\gamma$

$$\mathbf{A}^T(\theta_0) = \frac{\sigma(\pi/2 > \phi > 0) - \sigma(\pi > \phi > \pi/2)}{\sigma(\pi/2 > \phi > 0) + \sigma(\pi > \phi > \pi/2)},$$

Most important result

Measurement of $\mathbf{A}^T(\theta_0)$ directly probes $\text{Im} a_\gamma$, which is inaccessible without the use of transverse polarization,

- ▶ Using \mathbf{A}_T , **95%** CL simultaneous limit on the coupling $\text{Im} a_\gamma$ is 4.01×10^{-2} for $m_H = 120$ GeV,
- ▶ In principle, any odd function of $\sin 2\phi$ can probe $\text{Im} a_\gamma$,
- ▶ For example, $\text{sign}(\sin 2\phi) \equiv \mathbf{A}_T$, $\sin 2\phi$ and $\sin^3 2\phi$

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- ▶ To probe those couplings, we utilize momenta of leptons coming from **Z**-decay, to construct **T** odd observables.

Observables chosen for the analysis

Symbol	Observable	CP	T	Couplings
X_1	$(\mathbf{p}_1 - \mathbf{p}_2) \cdot \mathbf{q}$	-	+	$\text{Im}\tilde{\mathbf{b}}_Z, \text{Im}\tilde{\mathbf{b}}_\gamma$
X_2	$\mathbf{P} \cdot (\mathbf{p}_3 - \mathbf{p}_4)$	-	+	$\text{Im}\tilde{\mathbf{b}}_Z, \text{Im}\tilde{\mathbf{b}}_\gamma$
X_3	$(\vec{\mathbf{p}}_3 \times \vec{\mathbf{p}}_4)_z$	-	-	$\text{Re}\tilde{\mathbf{b}}_Z, \text{Re}\tilde{\mathbf{b}}_\gamma$
X_4	$(\mathbf{p}_1 - \mathbf{p}_2) \cdot (\mathbf{p}_3 - \mathbf{p}_4) (\vec{\mathbf{p}}_{1-} \times \vec{\mathbf{p}}_{1+})_z$	-	-	$\text{Re}\tilde{\mathbf{b}}_Z, \text{Re}\tilde{\mathbf{b}}_\gamma$
X_5	$(\mathbf{p}_1 - \mathbf{p}_2) \cdot \mathbf{q} (\vec{\mathbf{p}}_3 \times \vec{\mathbf{p}}_4)_z$	+	-	$\text{Im}\mathbf{b}_Z, \text{Im}\mathbf{b}_\gamma$
X_6	$\mathbf{P} \cdot (\mathbf{p}_3 - \mathbf{p}_4) (\vec{\mathbf{p}}_3 \times \vec{\mathbf{p}}_4)_z$	+	-	$\text{Im}\mathbf{b}_Z, \text{Im}\mathbf{b}_\gamma$
X_7	$[(\mathbf{p}_1 - \mathbf{p}_2) \cdot \mathbf{q}]^2$	+	+	$\text{Re}\mathbf{b}_Z, \text{Re}\mathbf{b}_\gamma$
X_8	$[(\mathbf{p}_1 - \mathbf{p}_2) \cdot (\mathbf{p}_3 - \mathbf{p}_4)]^2$	+	+	$\text{Re}\mathbf{b}_Z, \text{Re}\mathbf{b}_\gamma$

**THANK YOU FOR YOUR
ATTENTION**